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# Low temperature vibrational spectra, lattice dynamics, and phase transitions in some potassium hexahalometallates: $K_2[XY_6]$ with $X = \text{Sn}$ or $\text{Te}$ and $Y = \text{Cl}$ or $\text{Br}$

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This paper deals with the observation and identification of phonon frequencies resulting from the low temperature phase transitions in  $K_2XY_6$  crystals. By means of a simple lattice dynamical model, the vibrational Raman and IR data available in the literature and obtained here have been analyzed. The model used is an extension of one previously used to explain the vibronic spectra of several related compounds.

## INTRODUCTION

Many crystals of the composition  $K_2[XY_6]$ , with  $X = \text{metal (IV)}$  and  $Y = \text{halogen}$ , tend to adopt the cubic antiferroite ( $K_2[\text{PtCl}_6]$ -type) structure with space group  $Fm\bar{3}m$  ( $O_h^5$ ) at higher temperatures. During cooling, these crystals sometimes transform, via second order phase transitions, to lower symmetry pseudocubic structures. Well-investigated examples are the  $K_2[\text{ReCl}_6]$  and  $K_2[\text{SnCl}_6]$  crystals, which have four transitions, the first of which is considered<sup>1,2</sup> to originate from a condensation of a soft  $[XY_6]$  rotary mode at the zone center  $\Gamma$ , transforming the crystal symmetry to  $I4/m$  ( $C_{4h}^5$ ) at 110.9 K for Re and to  $P4/mnc$  ( $D_{4h}^6$ ) at 261 K for Sn.

The crystals  $K_2[\text{SnCl}_6]$  and  $K_2[\text{SnBr}_6]$  are known to be rigorously cubic  $Fm\bar{3}m$  ( $O_h^5$ ) at higher temperatures. At the temperatures  $T_{c1}$ , these crystals transform to tetragonal phases, which are stable in a relatively narrow temperature range (see Table I). After passing below the second transformation temperature  $T_{c2}$ , these crystals turn into a third phase, which is known to be monoclinic for  $K_2[\text{SnCl}_6]$ .<sup>2</sup>

The  $K_2[\text{TeCl}_6]$  crystal is monoclinic, though very nearly cubic, at room temperature. There is DTA indi-

cations of phase transitions at 332 and 339 K,<sup>8</sup> but it has not yet been proved that the high temperature phase is cubic  $O_h^5$ , as can be expected.

The situation in the  $K_2[\text{TeBr}_6]$  crystal is almost the same: It is monoclinic<sup>15</sup> at room temperature and also has transitions at higher temperatures (434 and 405 K),<sup>8</sup> as well as a transition at 243 K, indicated by nuclear quadrupole experiments.<sup>14</sup>

It has been suggested<sup>1</sup> that the tetragonal and monoclinic structures are obtained as the result of small rotations of the  $[XY_6]$  octahedra around one or another set of axes. To illustrate this, consider the very well-examined<sup>2,15</sup> distortions present in the monoclinic phase III of  $K_2[\text{SnCl}_6]$  or  $K_2[\text{TeBr}_6]$ . Basically, it is the cubic antiferroite lattice, but the following perturbations occur<sup>15</sup>:

- (i) a rotation of neighboring regular octahedra about the  $c$  axis by  $\sim 8^\circ$  for  $[\text{SnCl}_6]$  and  $\sim 12^\circ$  for  $[\text{TeBr}_6]$ , in alternating directions ("antiferro" rotations),
- (ii) a "ferro" rotation of all octahedra about the monoclinic  $b$  axis (cubic  $[110]$ ) by  $\sim 8^\circ$  and  $9^\circ$  in the same direction, followed by
- (iii) displacements of  $K^+$  ions and small adjustments

TABLE I. Phase transitions of  $K_2[XY_6]$  crystals. The known space groups and conversion temperatures (K) are indicated.

	Phase I (high temp.)	$T_{c1}$	Phase II	$T_{c2}$	Phase III
$K_2[\text{SnCl}_6]$ (Refs. 2-8)	$Fm\bar{3}m$ ( $O_h^5$ )	261	$P4/mnc$ ( $D_{4h}^6$ )	254	$P2_1/n$ ( $C_{2h}^5$ )
$K_2[\text{SnBr}_6]$ (Refs. 5-11)	$Fm\bar{3}m$ ( $O_h^5$ )	400	Tetragonal	375 <sup>b</sup>	lower than tetragonal; (Ref. 6) $D_4^4$ (Refs. 9 and 10)
$K_2[\text{TeCl}_6]^a$ [Refs. 8 and 12-14]	$Fm\bar{3}m$ ?	339	?	332	$C2/m$ ( $C_{2h}^3$ )
$K_2[\text{TeBr}_6]$ (Refs. 8, 14 and 15)	$Fm\bar{3}m$ ?	434	?	405	$P2_1/n$ ( $C_{2h}^5$ )

<sup>a</sup>A transition to a fourth phase stable below  $\sim 165$  K has been suggested.<sup>13</sup>

<sup>b</sup>Swanson<sup>11</sup> has  $368 \pm 5$  K.

of cell parameters.

The  $K_2[TeCl_6]$  crystal structure at room temperature<sup>12</sup> is simpler than that of  $K_2[TeBr_6]$ , as the former lacks the distortion type (i). However, based on the low temperature infrared and Raman Spectra, it has been suggested<sup>13</sup> that  $K_2[TeCl_6]$  has a phase transition near  $\sim 165 \pm 30$  K that results in some kind of unit cell multiplication.

On the other hand, the lower temperature phases of  $K_2[ReCl_6]$  and  $K_2[SnCl_6]$  are quite simple in that the type (i) antiferro rotations occur, but here without simultaneous type (ii) ferro rotations.

In 1970, O'Leary and Wheeler<sup>1</sup> established their lattice dynamical model for  $K_2[ReCl_6]$ , a model which quite successfully accounts for the observed low-temperature Raman and infrared spectral bands as well as analyzes the possible character of the phase transitions.

With their success in mind, it is tempting to try to construct and fit a similar model based on lattice dynamics for the  $K_2[SnY_6]$  and  $K_2[TeY_6]$  crystals, and this is done in the present paper. However, the situation here is slightly more difficult due to the initial monoclinic distortion in some of the crystals at room temperature, a feature which allows additional spectroscopic transitions to be observed. While this would normally be an advantage, the reduced symmetry also leads to splitting of degenerate "cubic" states. A simple lattice model based on octahedral symmetry alone will not be able to fit the additional bands resulting from the removal of the degeneracy. However, if the splitting is small, it may still be possible to use such a model to gain at least a qualitative understanding of the observed spectra.

## EXPERIMENTAL

### Experimental methods

Some missing experimental data concerning low temperature far IR and Raman spectra are provided in this section.

The compounds were prepared by standard methods: Freshly distilled pure  $TeCl_4$  and pure  $KCl$  were melted in equivalent amounts in silica ampoules, limiting the reaction with atmospheric moisture using dry-box techniques;  $SnCl_4$ ,  $SnBr_4$ , or  $TeO_2$  were dissolved in the corresponding concentrated acid and mixed with  $KCl$  or  $KBr$  aqueous solutions. The purities of the compounds were tested by volumetric analysis of halogen:

	calc	found
$K_2SnCl_6$	51.932%	$51.2\% \pm 0.3\%$
$K_2SnBr_6$	70.889%	$70.9\% \pm 0.3\%$
$K_2TeCl_6$	50.826%	$51.2\% \pm 0.3\%$
$K_2TeBr_6$	69.967%	$68.8\% \pm 0.3\%$

The methods used in obtaining the spectra have been described in detail.<sup>13</sup> The interferometric far IR technique was improved in two ways: (i) The heat conductivity of pressed discs of polyethylene was helped by covering the surface with paraffin oil and pressing onto

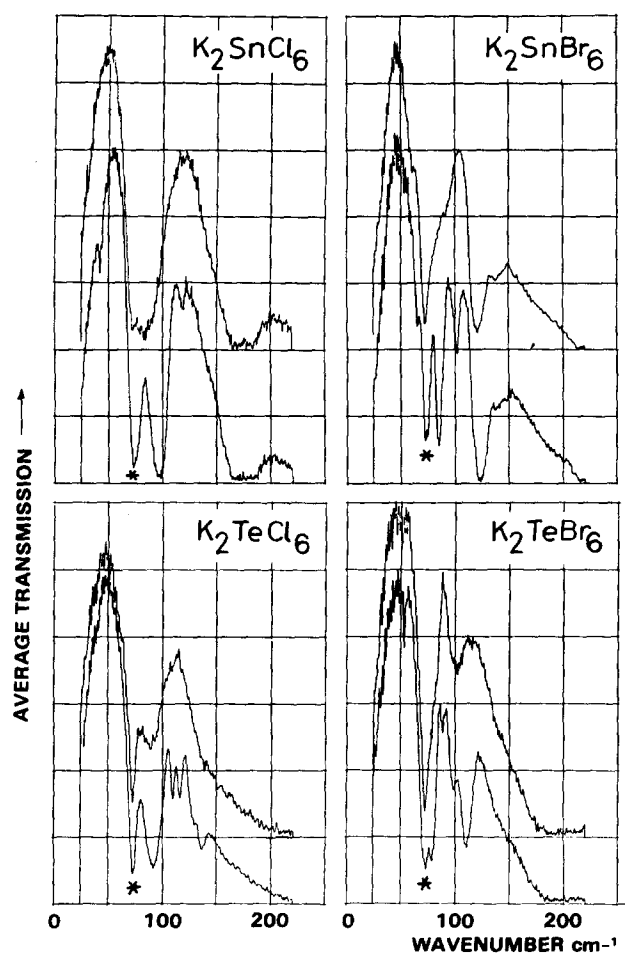


FIG. 1. Far infrared transmission spectra of  $K_2[XY_6]$  obtained at room temperature (upper spectra) and at  $\sim 100$  K. Resolution:  $0.7 \text{ cm}^{-1}$ . Finely dispersed powder in pressed polyethylene discs. The band at  $72 \text{ cm}^{-1}$  (marked with asterisk) is due to polyethylene.

a transparent silicon plate (from TOPSIL, Inc., Frederikssund, Denmark) in good contact along the whole periphery with the variably cold junction of the cryostat. The temperature was determined by an iron-constantan thermocouple. (ii) The double sided interferograms were corrected for drift and apodized using a squared sinus function prior to Cooley-Tukey fast Fourier transformation, done in a large computer with plotting facilities. Two or more spectra were finally averaged.

The true temperatures in the Raman experiments were estimated by recording the  $\nu_5$  mode on both the Stokes and anti-Stokes side and calculating the temperature from the ratio of integrated intensity, assuming Boltzmann's distribution. The temperatures determined in this way were reproducible within  $\pm 10$  K and were in general a few degrees higher than the copper block of the cryostat.

### Experimental results

The results of the experimental work are shown in Figs. 1 and 2 and in Table II. Some seven phonon frequencies can be considered as well established, and various hypothetical assignments for some of the rest

TABLE II. Experimental Raman and IR absorption data ( $\text{cm}^{-1}$ ) for  $\text{K}_2[\text{XY}_6]$  at 300 K or as indicated, in (approximately) cubic space group  $O_h^5 \equiv Fm\bar{3}m$ .

	K <sub>2</sub> SnCl <sub>6</sub>		K <sub>2</sub> SnBr <sub>6</sub>		K <sub>2</sub> TeCl <sub>6</sub>		K <sub>2</sub> TeBr <sub>6</sub>		Possible identifications based on this work		
Lattice constant (Å)	9.98		~10.54		~10.14		10.69				
X–Y bond length (Å)	2.407		~2.63		~2.54		2.71				
Raman	Well-established origin				469,	465 <sup>c</sup>					
	A <sub>1g</sub> (Γ <sub>1</sub> <sup>+</sup> , ν <sub>1</sub> )	324,	323.7 <sup>a</sup>	190,	190	297,	294 <sup>c</sup>	176,	177 <sup>c</sup>	A <sub>1g</sub> (Γ <sub>1</sub> <sup>+</sup> , ν <sub>1</sub> )	
	E <sub>g</sub> (Γ <sub>3</sub> <sup>+</sup> , ν <sub>2</sub> )	244,	245.8 <sup>a</sup>	144,	144	251,	251 <sup>c</sup>	154,	157 <sup>c</sup>	E <sub>g</sub> (Γ <sub>3</sub> <sup>+</sup> , ν <sub>2</sub> )	
	T <sub>2g</sub> (Γ <sub>5</sub> <sup>+</sup> , ν <sub>3</sub> )		177 <sup>a</sup>		116 <sup>e</sup>	142	149 <sup>c</sup>	99,	111 <sup>c</sup>	(X <sub>3</sub> <sup>+</sup> , ν <sub>5</sub> LO)	
		172,	172 <sup>a</sup>	109, <sup>d</sup>	110 <sup>e</sup>		144 <sup>c</sup>	92,	103 <sup>c</sup>	T <sub>2g</sub> (Γ <sub>5</sub> <sup>+</sup> , ν <sub>3</sub> )	
			164 <sup>a</sup>				137 <sup>c</sup>		94 <sup>c</sup>	X <sub>5</sub> <sup>+</sup>	
			104.4 <sup>a</sup>				109,	110 <sup>c</sup>			T <sub>1g</sub> +X <sub>4</sub> <sup>+</sup> ?
			96.6 <sup>a</sup>		88 <sup>e</sup>			101 <sup>c</sup>			T <sub>1g</sub> +X <sub>5</sub> <sup>+</sup> ?
	T <sub>2g</sub> (Γ <sub>5</sub> <sup>+</sup> , ν <sub>L</sub> )						84 <sup>c</sup>			T <sub>1g</sub> +T <sub>1g</sub> ?	
		~72,	81.0 <sup>a</sup>	82, <sup>d</sup>	80 <sup>e</sup>	70	76 <sup>c</sup>	74,	74 <sup>c</sup>	T <sub>2g</sub> (Γ <sub>5</sub> <sup>+</sup> , ν <sub>L</sub> )	
			84.5 <sup>a</sup>		75 <sup>e</sup>		93 <sup>c</sup>			X <sub>5</sub> <sup>+</sup>	
		54 <sup>b</sup>	69.8 <sup>a</sup>	64, <sup>f</sup>	57 <sup>e</sup>		68 <sup>c</sup>			T <sub>1g</sub> (X <sub>4</sub> <sup>+</sup> )	
			60.0 <sup>a</sup>	41, <sup>d</sup>	47 <sup>e</sup>	59,	60 <sup>c</sup>		48 <sup>c</sup>	T <sub>1g</sub> (X <sub>5</sub> <sup>+</sup> )	
			46.3 <sup>a</sup>			48,	47 <sup>c</sup>			T <sub>1g</sub>	
							43 <sup>c</sup>				
			37.8 <sup>a</sup>	23, <sup>d</sup>	33 <sup>e</sup>	36,	38 <sup>c</sup>		34 <sup>c</sup>		
Infrared			285,	288 <sup>c</sup>	312,	312 <sup>c</sup>					
	T <sub>1u</sub> (Γ <sub>4</sub> <sup>–</sup> , ν <sub>3</sub> )	~324 (TO: 314)	~225,	~225 <sup>c</sup>	~255,	~255	~195,	~195 <sup>c</sup>	T <sub>1u</sub> (Γ <sub>4</sub> <sup>–</sup> , ν <sub>3</sub> )		
	T <sub>1u</sub> (Γ <sub>4</sub> <sup>–</sup> , ν <sub>4</sub> )	~175	~121,	124 <sup>c</sup>	140,	136 <sup>c</sup>	100,	110 <sup>c</sup>	T <sub>1u</sub> (Γ <sub>4</sub> <sup>–</sup> , ν <sub>4</sub> )		
						128 <sup>c</sup>			X <sub>5</sub> <sup>–</sup>		
			118 <sup>c</sup>			115 <sup>c</sup>			T <sub>2u</sub> (X <sub>5</sub> <sup>–</sup> )		
						109 <sup>c</sup>			T <sub>2u</sub> (Γ <sub>5</sub> <sup>–</sup> )		
	T <sub>1u</sub> (Γ <sub>4</sub> <sup>–</sup> , ν <sub>L</sub> )				101 <sup>c</sup>			100 <sup>c</sup>	X <sub>4</sub> <sup>+</sup> +X <sub>4</sub> <sup>–</sup> ?		
			97 <sup>c</sup>					89 <sup>c</sup>	X <sub>5</sub> <sup>–</sup>		
						87,	97 <sup>c</sup>		X <sub>3</sub> <sup>–</sup>		
		84	74.8 <sup>c</sup>	78,	84 <sup>c</sup>		92 <sup>c</sup>	76,	79 <sup>c</sup>	T <sub>1u</sub> (Γ <sub>4</sub> <sup>–</sup> , ν <sub>L</sub> )	
							87 <sup>c</sup>			X <sub>5</sub> <sup>–</sup>	
					65 <sup>c</sup>					X <sub>2</sub> <sup>–</sup>	
							57 <sup>c</sup>			X <sub>4</sub> <sup>–</sup>	
								53 <sup>c</sup>		T <sub>1g</sub> +X <sub>5</sub> <sup>–</sup>	
		42.5 <sup>c</sup>				42 <sup>c</sup>			X <sub>5</sub> <sup>–</sup>		
	References	4		11, 19		13		19, 20			

<sup>a</sup>At  $\sim 50$  K.<sup>b</sup>Extrapolated to  $\sim 300$  K.<sup>c</sup>At  $\sim 100$  K.<sup>d</sup>At  $\sim 300$  K.<sup>11</sup><sup>e</sup>At  $\sim 95$  K.<sup>11</sup><sup>f</sup>At 300 K.<sup>9</sup>

can be guessed and tested by the subsequent calculations. All four systems have been studied before, but not all at lower temperatures.<sup>3,4,11,13,20</sup> The (reversible) evolution in the far IR spectra as the temperature is lowered

towards  $\sim 100$  K shows the following:

(i)  $\text{K}_2[\text{SnCl}_6]$ : weak, narrow bands appear near 42.5 and 118  $\text{cm}^{-1}$  at temperatures around  $\sim 200$  K. These

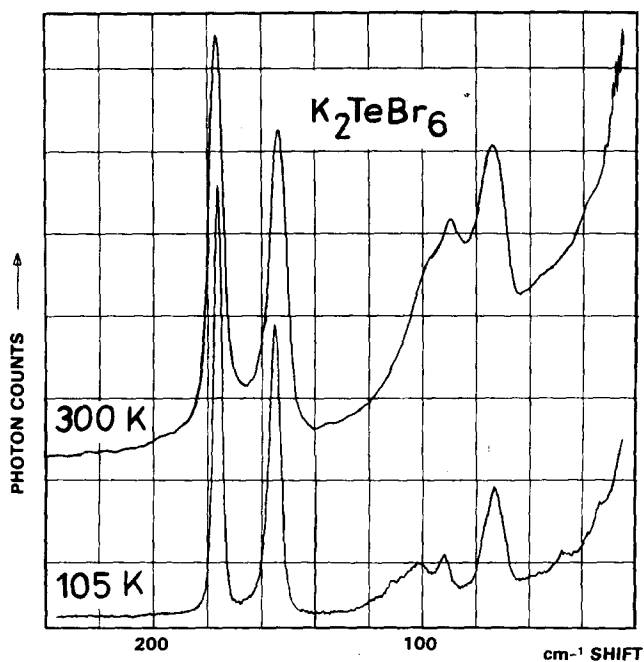


FIG. 2. Raman scattering spectra of  $K_2[TeBr_6]$  power obtained at the indicated temperatures. Resolution:  $2\text{ cm}^{-1}$ . Excited with  $\sim 20\text{ mW}$  of filtered  $16355\text{ cm}^{-1}$  dye laser radiation.

bands were stationary within experimental accuracy and disappeared reversibly by heating.

(ii)  $K_2[SnBr_6]$ : at  $\sim 240\text{ K}$ , a distinct shoulder emerges at  $\sim 92\text{ cm}^{-1}$ , moving to  $\sim 101\text{ cm}^{-1}$ , and gaining in intensity by cooling to  $\sim 100\text{ K}$ . At this temperature, weak bands at  $199$  and  $65\text{ cm}^{-1}$  are seen, and all features show reversibility.

(iii)  $K_2[TeCl_6]$ : two pronounced bands at  $115$  and  $109\text{ cm}^{-1}$  appear and disappear reversibly around  $165\text{ K}$ . In some spectra (but not in all), we observed weak bands at  $57$  and  $42\text{ cm}^{-1}$  at low temperatures.

(iv)  $K_2[TeBr_6]$ : there is a gradual evolution in the sharpness of bands by cooling. The  $53\text{ cm}^{-1}$  band is faintly observable at room temperature. The  $89$  and

$100\text{ cm}^{-1}$  bands can be weakly discerned around  $200\text{ K}$  and are distinct only below  $\sim 120\text{ K}$ .  $\nu_4$  shifts  $+10\text{ cm}^{-1}$ . The changes are reversible. Adams *et al.*<sup>20</sup> observed  $\nu_4$  at  $113\text{ cm}^{-1}$  and the band at  $55\text{ cm}^{-1}$  at  $120\text{ K}$  but did not resolve the bands at  $100$  and  $89\text{ cm}^{-1}$ .

The Raman spectra of three of the salts as a function of temperature are given in Refs. 3, 4, 11, 13. Characteristically, at low temperatures, all four salts show faint bands in the range below  $110\text{ cm}^{-1}$  and broad  $T_{2g}(\Gamma_5^-, \nu_5)$  bands (Table II and Fig. 2).

These spectral features at low temperatures must be associated with the phase transitions (Table I). It seems to be a general rule that the new spectral features do not necessarily appear immediately below the transformation point but must await a considerable distortion of the structure. As an example, in  $K_2[SnBr_6]$  with  $T_{c2} = 375\text{ K}$ , a lot of change is observed in the IR spectra between room temperature ( $300\text{ K}$ ) and  $100\text{ K}$  (Fig. 1). However, it is difficult to exclude a further transition to a phase IV ( $K_2[ReCl_6]$  has a  $T_{c3} = 76\text{ K}$ ), but at least in the Sn salts no indications of a  $T_{c3}$  has been seen using several different techniques.<sup>2-11</sup>

#### Lattice dynamical calculation

The lattice dynamical model used to generate the phonon dispersion curves for the compounds considered here is similar to the model used for  $Cs_2UBr_6$ <sup>16</sup> and  $Cs_2MnF_6$ .<sup>17,18</sup> Like O'Leary and Wheeler's model,<sup>1</sup> it is based on a parameterized force field acting between rigid ions. The model used here is characterized by a modified Urey-Bradley force field to describe the short range interactions within the  $XY_6$  complex plus additional short range terms to characterize the interactions with the potassium lattice and adjacent  $XY_6$  complexes. Added to this are the standard long range Coulomb terms.

A major problem with models of this type is to keep the number of adjustable parameters at a reasonably low level. Equation (1) gives the short range potential  $\phi^{SR}$  in terms of internal bond coordinates out to second nearest neighbor intercell Y-Y interactions:

$$\begin{aligned}
 2\phi^{SR} = & K \sum_I (\Delta r_i)^2 + F \sum_{II} (\Delta r_{ij})^2 + H r_0^2 \sum_{III} (\Delta \theta_{ijk})^2 \\
 & + K_2 \sum_{IV} (\Delta r_{ik})^2 + K_3 \sum_V (\Delta r_{il})^2 + K_4 \sum_{VI} (\Delta r_{im})^2 + K_{rr} \sum_{VII} (\Delta r_i)(\Delta r_j) + K_5 \sum_{VIII} (\Delta r_{kk'})^2 + K_{\theta\theta} \sum_{IX} (\Delta \theta_{ijk})(\Delta \theta_{ilm}) \\
 & + 2r_0 f' \sum_I (\Delta r_i) + 2R_1 F' \sum_{II} (\Delta r_{ij}) + 2R_2 k_2 \sum_{IV} (\Delta r_{ik}) + 2R_3 k_3 \sum_V (\Delta r_{il}) + 2R_4 k_4 \sum_{VI} (\Delta r_{im}) + 2R_5 k_5 \sum_{VIII} (\Delta r_{kk'}), \quad (1)
 \end{aligned}$$

where the sums run over I = X-Y pairs, separated by  $r_i$ ; II = Y-Y nearest neighbor pairs in same complex, separated by  $r_{ij}$ ; III = Y-X-Y angles  $\theta_{ijk}$ ; IV = K-Y nearest neighbor pairs, at  $r_{ik}$ ; V = Y-Y intercell nearest neighbor pairs, at  $r_{il}$ ; VI = Y-Y intercell next nearest neighbor pairs, at  $r_{im}$ ; VII = *trans*-X-Y bonds; VIII = K-K nearest neighbor pairs, at  $r_{kk'}$ ; IX = Y-X-Y angles with a common side; and where  $\Delta$  denote change from equilibrium values, which are  $r_0$  for the X-Y bond,  $R_1$

for the Y-Y nearest neighbor distance  $= \sqrt{2}r_0$ ,  $R_2$  for the K-Y distance  $\geq \sqrt{2}r_0$ ,  $R_3$  for the Y-Y intercell nearest distance  $\geq \sqrt{2}r_0$ ,  $R_4$  for the second neighbor intercell Y separation  $2r_0$ , and  $R_5$  for the K-K distance  $\geq 2r_0$ . The cell referred to here is the cube defined by the K ions, surrounding  $[XY_6]^{2-}$ .

The linear terms in Eq. (1) appear since the internal coordinates chosen are not independent. These terms

are related to the "perpendicular" force constants of O'Leary and Wheeler.<sup>1</sup> In equilibrium, forces on any atom must vanish. This is true by symmetry for all but the Y atoms. If we differentiate the total potential  $\phi^{\text{SR}} + V^{\text{Coul}}$  with respect to the Y position coordinates, the result must equal zero. This gives the following relation between the linear short range terms (assuming that the Y's are at the center of the face formed by the K atoms):

$$f' + 4(F' - k_3) = -\frac{\delta V^{\text{Coul}}}{\delta Y_Y} \quad (2)$$

where  $\delta V^{\text{Coul}}/\delta Y_Y$  is the space derivative of the Coulomb part of the potential with respect to the Y atom. This last term was evaluated using Ewalds theta function transformation with the atomic charges as parameters, these being related by

$$2q_K + q_X - 6q_Y = 0.$$

Previously, in an effort to reduce the number of parameters, the short range interaction between halogen atoms Y in adjacent complexes was neglected. Except for the Coulomb terms, all of the intercell interactions in these models was conveyed by the quadratic K-Y interaction parameter  $K_2$ .

The effect of this procedure has been to limit the dispersion and to affect the position of the  $T_{1g}$  mode.

The effect on dispersion of neglecting some of the intercell constants is illustrated by the second nearest neighbor linear Y-Y intercell parameter ( $k_4$ ). An interesting effect of this force constant is that it allows a splitting of  $T_{1g}$  and  $X_4^+$ . It is the only constant that does this. Because of its neglect, the  $T_{1g}$  and  $X_4^+$  modes will always be nearly degenerate in our model. This is in contrast to the findings of O'Leary and Wheeler, and emphasizes the effect of the second nearest neighbor Y-Y intercell coupling. The  $X_4^+$  mode is of particular interest since it has been identified as one of the soft modes in the  $K_2[\text{ReCl}_6]$  system.<sup>1</sup>

The  $T_{1g}$  mode is rather sensitive to the parameters of the model, and difficulties with it have been noted before. Additional freedom in fitting this mode is gained by adding either the linear K-Y interaction parameter  $k_2$  or adding the quadratic Y-Y second nearest neighbor intercell parameter  $K_4$ . These two parameters allow the  $T_{1g}$  mode to be moved relative to the other  $\Gamma$  point modes. We have chosen to only use  $K_4$  as it has the least effect on the other  $k=0$  modes. It should be noted that the nearest neighbor intercell Y-Y parameters ( $K_3, k_3$ ) do not help in fitting any  $k=0$  mode as they enter all modes in a linear combination with the Y-Y nearest neighbor intracell parameters ( $F, F'$ ) as  $F + K_3$  and  $F' + k_3$ . This is to be expected since, for the halogen positions assumed, we are just adding the two "springs" in series for the  $k=0$  modes. More importantly, the nearest neighbor intercell Y-Y distance does not change during a  $T_{1g}$  displacement. Because of this, these parameters were not used.

The parameter  $K_{rr}$  was retained because it aids in fitting the internal bond stretching modes of the  $[\text{XY}_6]$  complex ( $A_{1g}$ ,  $E_g$ , and the highest  $T_{1u}$ ). The parameter  $k_{\theta\theta}$  is sometimes added to the Urey-Bradley force field

to help in fitting the internal bending modes in the  $[\text{XY}_6]$  complex ( $T_{2g}$ ,  $T_{2u}$ , and second  $T_{1u}$ ). However, it was not needed for the compounds considered here. The parameters  $F'$ ,  $k_2$ , and  $k_{\theta\theta}$  tend to cause deviation from the well-known  $\nu_8 = \nu_5/\sqrt{2}$  result of the simple valence force field.

In this work, we have eliminated the following parameters: the nearest neighbor intercell Y-Y interaction ( $K_3, k_3$ ); the linear Y-Y second nearest neighbor intercell interaction ( $k_4$ ); the linear K-K interaction ( $k_5$ ); and  $K_{\theta\theta}$  and  $k_2$ .  $f'$  was calculated by Eq. (2). This leaves 10 parameters. While all 10 parameters were used in fitting  $K_2\text{TeCl}_6$ , only eight were used for the other compounds. This was accomplished by fixing  $F' = -0.1F$  and  $q_K = 1.0$ .

## DISCUSSION OF LATTICE DYNAMICAL MODEL CALCULATIONS

### General

The procedure used in fitting the parameters of the model was to start with selected "well established" modes. These were generally the  $k=0$ , room temperature modes which could usually be established by the systematics of these compounds. These are given in the left hand column of Table II. Based on these initial fittings, zone boundary phonons were identified that corresponded to the additional bands of the low temperature structure. As a check on the method, only  $k=0$  modes and odd phonons at the point X (i.e., the additional IR data) were used in fitting the parameters of the model. The even phonons at X could then be calculated and compared to the additional low temperature Raman data.

Tables III and IV give the results of several attempts at fitting the four compounds considered here. Figure 3(a)-3(d) show the calculated dispersion curves. For clarity, only the phonons below  $200 \text{ cm}^{-1}$  are displayed. The dynamical matrix was diagonalized only at the points  $\Gamma$ , X, and L in the Brillouin zone. The dispersion curves along  $\Delta$  and  $\Lambda$  are only approximate, being estimated from compatibility conditions and from the noncrossing of phonon branches of the same symmetry.

### $K_2[\text{SnCl}_6]$

The Raman spectra of this compound have been investigated by Pelzl *et al.*<sup>4</sup> in the neighborhood of the structural phase transitions. Their temperature dependent data show two soft modes that were identified as the  $\Gamma$  and X point rotational mode ( $T_{1g}$  and  $X_4^+$ ). Additional low frequency bands ( $105\text{--}38 \text{ cm}^{-1}$ ) appearing below the transition temperature were observed and associated with zone boundary phonons. The internal  $T_{2g}$  mode was also observed to undergo a "splitting" into three components below the transition.

In our work, we have observed additional IR bands below the phase transition. These data are summarized in Table II.

We have fit several models to the data, making various assumptions as to the origins of the observed lines.

TABLE III. Frequencies calculated for various selected models, fitting the approximate observed values (in parentheses) ( $\text{cm}^{-1}$ ).

Mode	$\text{K}_2[\text{SnCl}_6]$		$\text{K}_2[\text{SnBr}_6]$		$\text{K}_2[\text{TeCl}_6]$		$\text{K}_2[\text{TeBr}_6]$	
	Model 6	Model 7	Model 6	Model 7	Model 6	Model 7	Model 2	Model 3
$A_{1g}(\Gamma^{1g})\nu_1$	323.6 (324)	323.6 (324)	188.8 (190)	189.2 (190)	296.5 (297)	296.5 (297)	177.9 (177)	178.2 (177)
$E_g(\Gamma^{3g})\nu_2$	244.1 (244)	244.3 (244)	144.9 (144)	144.6 (144)	251.4 (251)	251.4 (251)	156.1 (157)	155.7 (157)
$T_{2g}(\Gamma^{5g})\nu_3$	174.5 (172)	174.3 (172)	111.9 (110)	111.3 (110)	143. (142)	146.2 (144)	103.5 (103)	103.9 (103)
$T_{2g}(\Gamma^{5g})\nu_L$	72.1 (72)	80.2 (80)	79.9 (80)	80. (80)	70.6 (70)	71.2 (72)	74.2 (74)	74. (74)
$T_{1g}(\Gamma^{4g})\nu_L$	43.2 (43)	42.2 (43)	46.1 (47)	32.6 (33)	43.5 (44)	42.8 (43)	48.1 (48)	34. (34)
$T_{1u}(\Gamma^{4u})\nu_3$	324.2 (324)	324.2 (324)	225. (225)	255. (255)	255. (255)	255. (255)	195. (195)	194. (195)
$T_{1u}(\Gamma^{4u})\nu_4$	171.8 (175)	172 (175)	122.7 (121)	122. (121)	133.4 (136)	134. (136)	109. (100.)	108.7 (110)
$T_{2u}(\Gamma^{5u})\nu_6$	115.6	115.5	72.6 (77)	73.8 (77)	101.1	106.9 (109)	70.5	72.2
$T_{1u}(\Gamma^{4u})\nu_L$	86.8 (84)	86.9 (84)	76.9 (78)	76.9 (84)	93. (92)	93.7 (92)	79. (79.)	79.4 (79)
$X_3^-$	113.5	113.3	78.4	75.	98.6 (97)	102.9	74.9	72.8
$X_2^-$	72.5 (74.8)	72.5 (74.8)	67.3 (65)	66.8 (65)	78.7	81.7	69.5	69.6
$X_4^-$	323.5	323.4	226.4	225.3	253.9	253.9	200.2	196.
$X_4^-$	178.	178.4	129.	124.7	141.4	138.7	114.3	110.9
$X_4^-$	52.	52.	41.9	38.7	56. (57)	54.3 (57)	41.2	37.9
$X_5^-$	323.8	323.8	225.6	225.	254.4	254.5	197.1	195.4
$X_5^-$	170.4	170.6	124.	121.7	130.2 (128)	128.8 (128)	110.6	107.8
$X_5^-$	118.9 (118)	119. (118)	88.	90.	106.3 (109)	109.7	84.	84.
$X_5^-$	85.1	91.8	78.	76.5	86.5 (87)	87.9 (87)	74.1	74.7
$X_5^- \text{ TA}$	38.3 (42.5)	38 (42.5)	29.	28.2	42.3 (42)	42.1 (42)	26.8	27.6
$\nu_3 \text{ LO}$	327.	327.	230.9	227.7	260.1	258.9	210.	200.
$\nu_4 \text{ LO}$	185.8	186.2	132.	132.3	175.3	173.9	123.	126.
$\nu_L \text{ LO}$	129.7	129.8	111.5	113.9	117.5	115.2	107.	105.3

Only the  $k=0$  and three new low temperature IR bands (74.8, 42.5, and 118  $\text{cm}^{-1}$ ) were used in the fitting. The results of our calculations are displayed in Table III and IV while the dispersion curves are shown in Fig. 3(a).

Based on these model calculations, we have made the mode identifications of Table II (right hand column). It should be observed that these identifications differ considerably from those of Pelzl *et al.*<sup>4</sup>

The splitting of the internal  $T_{2g}$  mode at 177  $\text{cm}^{-1}$  can be explained as being due to the appearance of the zone boundary phonons  $X_3^+$  and  $X_5^+$ . This identification seems more likely, as a splitting of the internal mode would

indicate a distortion of the  $\text{SnCl}_6$  octahedron. The two Raman lines at 104.4 and 96.6  $\text{cm}^{-1}$  are more difficult to explain as our calculations indicate no even symmetry phonons from the points  $X$  or  $\Gamma$  in this region (although an  $L_1^+$  mode occurs  $\sim 100 \text{ cm}^{-1}$ ). Pelzl's identifications of these modes as being due to an  $X_5^+$  and  $X_3^+$  component of the lattice  $T_{2g}$  mode must be in error. The  $X_3^+$  mode is uniquely determined by symmetry and is a longitudinal component of the internal  $T_{2g}$  mode and only involves Cl motion. Because of the above, we believe these two bands (which are only observed below 150 K) to be two phonon features, a possible identification being  $X_4^+ + T_{1g}$  ( $70 + 38 = 108 \text{ cm}^{-1}$ ) and  $X_5^+ + T_{1g}$  ( $58 + 38 = 96 \text{ cm}^{-1}$ ).

TABLE IV. Force field model parameters.

	Model	$K^a$	$F$	$F'$	$H$	$K_2$	$K_4$	$K_5$	$K_{rr}$	$Q_r$	$Q_k$
$\text{K}_2[\text{SnCl}_6]$	7	1.13	0.242	-0.0242 <sup>b</sup>	-0.0077	0.0551	-0.00456	-0.0181	-0.0421	-0.418	1.0
	6	1.12	0.224	-0.0234 <sup>b</sup>	-0.00734	0.0549	-0.00438	-0.0250	-0.0421	-0.413	1.0
$\text{K}_2[\text{SnBr}_6]$	6	0.951	0.163	-0.0163 <sup>b</sup>	0.0071	0.0449	0.0082	-0.00793	-0.0136	-0.474	0.952
	7	0.885	0.178	-0.0178 <sup>b</sup>	0.0167	0.0464	0.000573	-0.00962	-0.0207	-0.411	1.0
$\text{K}_2[\text{TeCl}_6]$	7	0.954	0.124	-0.0008	0.0159	0.0695	-0.00635	-0.0400	0.222	-0.433	1.14
	6	0.976	0.115	-0.00323	0.0107	0.0693	-0.00486	-0.0406	0.223	-0.461	1.19
$\text{K}_2[\text{TeBr}_6]$	2	1.02	0.0435	-0.00435 <sup>b</sup>	0.0393	0.0478	0.00477	-0.0188	0.219	-0.554	1.0
	3	0.909	0.0690	-0.0069 <sup>b</sup>	0.0545	0.0480	-0.00076	-0.0165	0.206	-0.439	1.0

<sup>a</sup>In  $\text{mdyne}/\text{\AA}$ .

<sup>b</sup> $F' = -F/10$ .

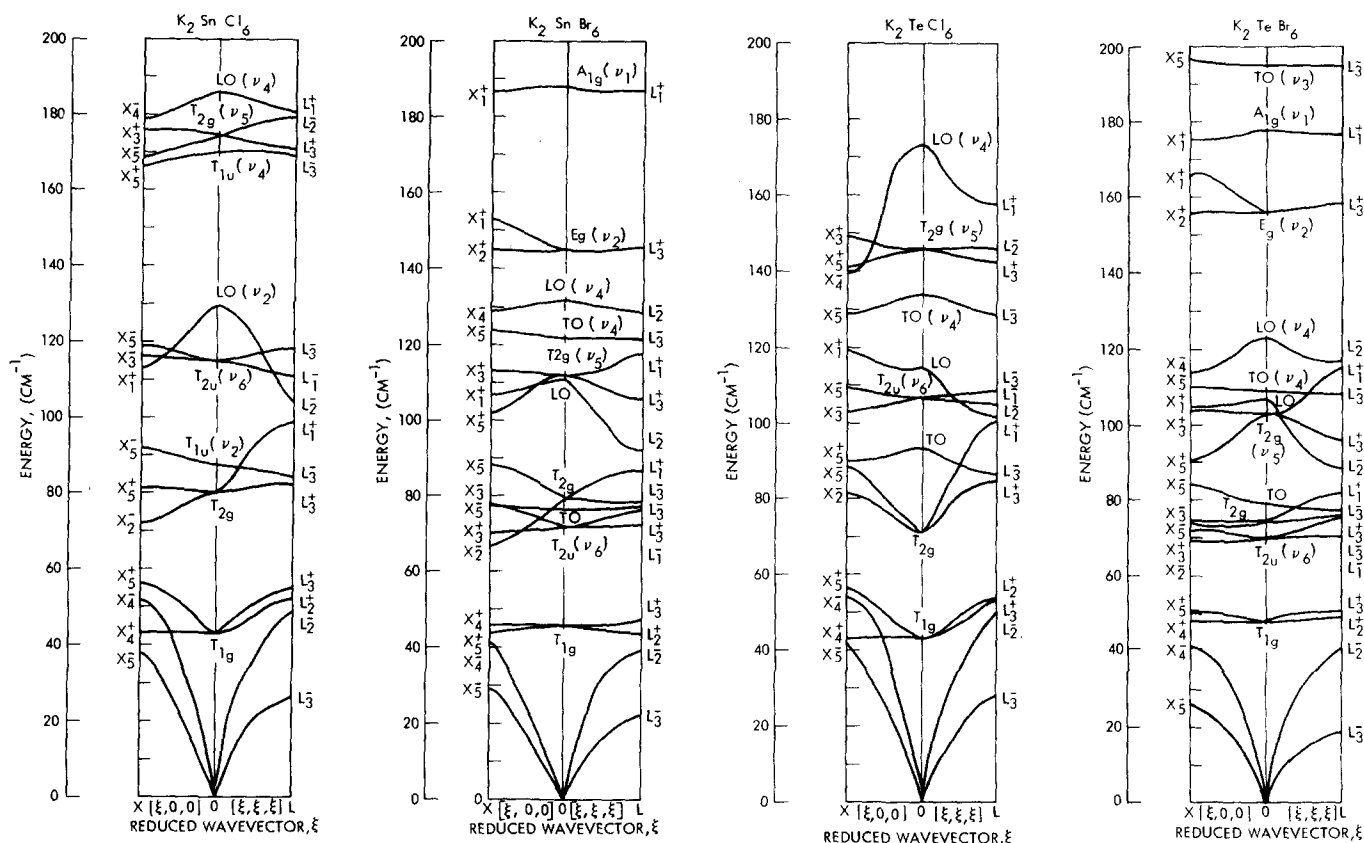


FIG. 3. Calculated dispersion curves: (a)  $K_2SnCl_6$  (model 7), (b)  $K_2SnBr_6$  (model 6), (c)  $K_2TeCl_6$  (model 7), (d)  $K_2TeBr_6$  (model 2). The parameters used were those of Table IV and the results are contained in Table V.

Our results indicate a slight separation between the  $T_{2g}$ ,  $k=0$  lattice mode and its  $X_5^+$  component. We believe these to be associated with the bands at 80 and  $84.5\text{ cm}^{-1}$ , respectively.

In our fitting of the parameters of the model, initial identifications were made using the room temperature data. Based on the dispersion curves of these early fittings, zone boundary phonons were correlated to the bands appearing in the low temperature spectra. The fits of Table III and IV are representative of this. In model 6, the  $T_{2g}$  band was placed at  $72\text{ cm}^{-1}$ . This band is observed to shift to  $80\text{ cm}^{-1}$  with temperature. Model 7 was run with  $T_{2g}$  at  $80\text{ cm}^{-1}$ . This caused the  $X_5^-$  component of the  $T_{1u}$  to shift from  $85$  to  $92\text{ cm}^{-1}$  (the  $T_{1u}$  was held at  $84\text{ cm}^{-1}$ ). This shift toward higher  $\text{cm}^{-1}$  corresponds to observed IR behavior in the region  $74\text{--}98\text{ cm}^{-1}$ . The parameters that changed most between Model 6 and 7 were  $K_5$ , the K-K interaction, and  $F$  and  $F'$ , the internal Cl-Cl constants. There was no calculated shift in the soft  $T_{1g}(X_5^+)$  and  $T_{1g}(X_4^+)$  modes. This is to be expected considering the way these parameters enter the model.

#### $K_2[SnBr_6]$

From the results summarized in Table I,  $K_2SnBr_6$  has  $O_h^5$  symmetry above  $400\text{ K}$ . Below this, it passes through a tetragonal phase with symmetry  $D_4^2$ . This space group is not a subgroup of  $O_h^5$  and cannot be reached with a distortion of symmetry of a point X phonon. Because of this, the analysis using zone boundary phonons is not

strictly valid in this case. However, it is believed that the  $O_h^5$  zone boundary X point phonons are a good approximation to the position of  $D_4^2$  phonons.

The temperature dependence of the data shows that  $T_{1u}$  shifts to higher energy as the temperature decreases ( $78\text{--}84\text{ cm}^{-1}$ ). Also, the  $T_{2g}$  mode apparently shifts from  $82$  to  $88\text{ cm}^{-1}$ .

The  $D_4^2$  space group lacks inversion symmetry. Anthonson<sup>11</sup> used this to explain the low temperature Raman band at  $116\text{ cm}^{-1}$  as being due to the  $T_{1u}$  mode. We see no other Raman band appearing in the IR.

We initially attempted to fit the room temperature data. Based on this, a low temperature IR band at  $65\text{ cm}^{-1}$  was identified as being due to  $X_2^-$ . This was used in fit model 6. No other  $k \neq 0$  phonons were used. The results of the calculation are displayed in Table III and IV, while the dispersion curves are shown in Fig. 3(b).

Without using the lack of inversion symmetry, we have identified the  $116\text{ cm}^{-1}$  band as being the  $X_3^+$  component of  $T_{2g}$ . Several features were accounted for as possible two phonon events. These were the  $101\text{ cm}^{-1}$  IR band as being  $X_4^+ + X_4^-$  ( $57 + 42 = 99$ ) or  $X_5^-$ , the  $88\text{ cm}^{-1}$  Raman band as  $T_{2g}$  or  $X_4^+ + T_{1g}$  ( $57 + 33 = 90$ ), and the  $80\text{ cm}^{-1}$  band as  $T_{2g}$  or  $T_{1g} + X_5^+$  ( $33 + 47$ ).

#### $K_2[TeCl_6]$

In fitting the data for this compound, initial attempts were made using the  $k=0$  modes. As the work pro-



gressed, 13  $k=0$  and odd symmetry  $X$  point phonons were identified and used in the model. The number of parameters was increased to ten, i. e., the conditions  $F' = -F/10$  and  $Q_X = 1$ , were not enforced.

The results of the model fitting are displayed in Tables III and IV while the phonon dispersion curves are shown in Fig. 3(c). Table II lists the final identifications based on the model. Model 7 was a special attempt to force the  $T_{2u}$  mode to the  $109\text{ cm}^{-1}$  region.

As with the cases of  $K_2[\text{SnCl}_6]$  and  $K_2[\text{SnBr}_6]$ , it was necessary to explain some of the features as two phonon combinations. These included the bands at  $110\text{ cm}^{-1}$  ( $T_{1g} + X_4^+ = 44 + 68$ ),  $101\text{ cm}^{-1}$  ( $T_{1g} + X_5^+ = 44 + 60$ ), and  $84\text{ cm}^{-1}$  ( $T_{1g} + T_{1g} = 44 + 44$ ).

This compound appears to show splitting of the lattice  $T_{2g}$  and the  $T_{1g}$  modes due to the lowered symmetry. The  $X_4^+$  mode was picked as the band at  $68\text{ cm}^{-1}$  due to this mode always being  $5\text{--}10\text{ cm}^{-1}$  higher in energy than the  $X_5^+$ .<sup>1,4</sup> It should be noted that the  $68\text{ cm}^{-1}$  band could also be due to the  $T_{2g}$  mode splitting.

### $K_2[\text{TeBr}_6]$

$K_2[\text{TeBr}_6]$  has symmetry  $C_{2h}^5$  below  $405\text{ K}$ , a transition to a lower symmetry below  $243\text{ K}$  is indicated by nuclear quadrupole experiments.<sup>14</sup> The spectra of Table II shows corresponding bands in the IR and Raman ( $110$ ,  $100$ , and  $55\text{ cm}^{-1}$ ). While the possible loss of inversion symmetry cannot be ruled out, we believe it to be accidental.

Eight  $k=0$  frequencies were identified and used in the models of Tables III and IV. The dispersion curve of model 2 is displayed in Fig. 3(d). Model 3 was an attempt to move the  $T_{1g}$  band to  $34\text{ cm}^{-1}$ .

Table II shows the identification based on these models. The Raman and IR coincidences are probably due to  $T_{1u}$  and  $X_3^+$  ( $X_1^+$ ) ( $110\text{ cm}^{-1}$ ),  $T_{2g}$  and  $X_4^+ + X_4^-$  ( $100\text{ cm}^{-1}$ ), and  $X_4^+(X_5^+)$  and  $T_{1g} + X_5^-$  ( $55\text{ cm}^{-1}$ ). Generally, the fits and identifications for  $K_2[\text{TeBr}_6]$  are the least satisfying.

### CONCLUSION

The Raman and infrared spectra accompanying the phase transitions in four hexachloro- and hexabromometallates have been investigated. Where data was not available from the literature, new spectra were taken. The results of a simple lattice dynamical calculation

show that all new bands appearing in the spectra can be explained in terms of zone boundary phonons from the point  $X$  becoming allowed due to unit cell doubling. Several misidentifications appearing in previous works have been corrected.

A shortcoming of our lattice model in predicting the soft  $T_{1g}$  and  $X_4^+$  modes has been investigated and traced to the omission of second intercell nearest neighbor interactions.

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